

CLAIMS

What is claimed is:

1. A method of modeling failure of a borehole in a subsurface formation, the method comprising:
 - (a) defining a subsurface model including a plurality of regions, said plurality of regions including the borehole and at least one additional region selected from (i) a liner in the borehole, (ii) a casing in the borehole, and (iii) at least one earth formation, each of said plurality of regions comprising a plurality of nodes interconnected by a plurality of linkages,
 - (b) defining material properties associated with said nodes and said linkages of said subsurface model, said material properties having a statistical variation;
 - (c) specifying an initial deformation pattern of the model; and
 - (d) using a dynamic range relaxation algorithm (DRRA) to find a force equilibrium solution for said subsurface model and said initial deformation pattern giving a resulting deformed model including fracturing.
2. The method of claim 1, wherein said nodes are arranged in a grid that is one of (i) a triangular grid, and, (ii) a random grid.
3. The method of claim 1 wherein said linkages are selected from the group consisting of (A) springs, (B) beams, and, (C) rods.

- 1 4. The method of claim 1 wherein said linkages comprise springs, the method
2 further comprising defining a normal force associated with each spring.
- 1 5. The method of claim 1 wherein said linkages comprise beams, the method
2 further comprising defining at least one of (A) a normal force, and (B) a shear
3 force associated with each beam.
- 1 6. The method of claim 1 wherein said linkages comprise rods, the method
2 further comprising defining at least one of (A) a normal force and (B) a force
3 associated with an angle between pairs of said adjacent ones of the plurality of
4 rods.
- 1 7. The method of claim 1, wherein using the dynamic range relaxation algorithm
2 further comprises applying said initial deformation model in a plurality of
3 steps, each step comprising applying a specified fraction of the initial
4 deformation and determining if any linkages between the nodes have been
5 deformed beyond a breaking point and identifying a subset of the linkages that
6 have been so deformed.
- 1 8. The method of claim 7, wherein applying the dynamic range relaxation
2 algorithm further comprises iteratively breaking the one linkage of the subset
3 of linkages that has been deformed the most and applying a relaxation
4 algorithm to the remaining unbroken linkages.

1 9. The method of claim 9 wherein the at least one earth formation further
2 comprise a near earth formation including a gravel pack and a far earth
3 formation.

1 10. The method of claim 1 wherein the plurality of regions comprises a liner in the
2 borehole, an earth formation including a near earth formation and a far earth
3 formation, and a gravel pack disposed between the liner and the near earth
4 formation.

1 11. The method of claim 1 wherein said linkages connect at least one selected
2 node of said plurality of nodes with (i) a plurality of nearest neighbors of the
3 at least one selected node, and (ii) a plurality of next nearest neighbors of the
4 at least one selected node.

1 12. The method of claim 1 wherein said earth formations include a fluid, said fluid
2 flowing into the borehole, and said deformation pattern is determined in part
3 by a decrease in formation fluid pressure resulting from flow of said fluid into
4 the borehole.

1 13. The method of claim 12 wherein using the DRRA further comprises
2 determining an additional force at each node related to a difference in said
3 fluid pressure on opposite sides of at least a subset of the plurality of nodes.

- 1 14. The method of claim 13 wherein determining said additional force further
2 comprises performing a simulation selected from (i) a finite difference
3 simulation, and, (ii) a finite element simulation, of said fluid flow.
- 1 15. The method of claim 14 wherein performing said simulation further comprises
2 changing at least one of (A) a permeability, and, (B) a porosity used in said
3 simulation responsive to said deformation.
- 1 16. The method of claim 1 wherein said borehole includes a substantially vertical
2 section wherein said initial deformation pattern is substantially azimuthally
3 symmetric about an axis of the borehole in said section.
- 1 17. The method of claim 16 wherein said borehole includes a deviated section
2 wherein said initial deformation pattern is asymmetrical about an axis of the
3 borehole.
- 1 18. A method of modeling failure of a borehole in a subsurface formation, the
2 method comprising:
3 (a) defining a subsurface model having a plurality of nodes and including
4 a plurality of regions, said plurality of regions including the borehole
5 and at least one additional region selected from (i) a liner in the
6 borehole, (ii) a casing in the borehole, and (iii) at least one earth
7 formation, each of said plurality of regions comprising a plurality of
8 nodes interconnected by a plurality of linkages,

- 9 (b) defining material properties associated with said nodes and said
10 linkages of said subsurface model, said material properties having a
11 statistical variation;
- 12 (c) specifying a force distribution applied to the model at boundary nodes
13 of said plurality of nodes; and
- 14 (e) using a dynamic range relaxation algorithm (DRRA) to find a force
15 equilibrium solution for said subsurface model and said force
16 distribution giving a resulting deformed model including fracturing.

1 19. The method of claim 18 wherein the subsurface formation has been subjected
2 to large scale geologic deformation and wherein specifying said force
3 distribution further comprises:

- 4 (i) simulating the large scale geologic deformation to determine a stress
5 distribution in the subsurface formation in the absence of the borehole,
6 (ii) defining a trajectory for the borehole therein, and
7 (iii) identifying locations along said trajectory that are likely to fail.

1 20. The method of claim 18 wherein the forces can vary between the boundary
2 nodes.

1 21. The method of claim 19 wherein identifying said trajectories further comprises
2 removing a plurality of nodes along said trajectory.

1 22. The method of claim 18, wherein said nodes are arranged in a grid that is one

2 of (i) a triangular grid, and, (ii) a random grid.

1 23. The method of claim 18 wherein said linkages are selected from the group
2 consisting of (A) springs, (B) beams, and. (C) rods.

1 24. The method of claim 18 wherein said linkages comprise springs, the method
2 further comprising defining a normal force associated with each spring.

1 25. The method of claim 18 wherein said linkages comprise beams, the method
2 further comprising defining at least one of (A) a normal force, and (B) a shear
3 force associated with each beam.

1 26. The method of claim 18 wherein said linkages comprise rods, the method
2 further comprising defining at least one of (A) a normal force and (B) a force
3 associated with an angle between pairs of said adjacent ones of the plurality of
4 rods.

1 27. The method of claim 18, wherein using the dynamic range relaxation
2 algorithm further comprises applying said force distribution in a plurality of
3 steps, each step comprising applying a specified fraction of the force and
4 determining if any linkages between the nodes have been deformed beyond a
5 breaking point and identifying a subset of the linkages that have been so
6 deformed.

1 28. The method of claim 27, wherein applying the dynamic range relaxation
2 algorithm further comprises iteratively breaking the one linkage of the subset
3 of linkages that has been deformed the most and applying a relaxation
4 algorithm to the remaining unbroken linkages.

1 29. A method of modeling faulting and fracturing in a subsurface volume of the
2 earth comprising:

- 3 (a) defining said subsurface model including a plurality of interconnected
4 nodes and material rock properties within the subsurface volume;
5 (b) specifying a stress distribution at a subset of said plurality of nodes,
6 said subset comprising boundary nodes; and
7 (c) using a dynamic range relaxation algorithm to find a force equilibrium
8 solution for said subsurface model and said stress distribution giving a
9 resulting deformed model including fracturing.

1 30. The method of claim 29, wherein defining a subsurface model, and specifying
2 said stress distribution further comprises using a graphical user interface.

1 31. The method of claim 29, wherein said nodes are arranged in a grid that is one
2 of (i) a triangular grid, and, (ii) a random grid.

1 32. The method of claim 29, wherein said nodes are interconnected by linkages
selected from (i) springs, (ii) beams, and, (iii) rods.